

Algorithm 4.6.1**The CYK algorithm**

input: context-free grammar $G = (V, \Sigma, P, S)$

string $u = x_1x_2 \dots x_n \in \Sigma^*$

private:

X : a table containing sets of variables

$step$: the index of the “diagonal”, the main diagonal is 1, the one above it is 2, and so on.

i : row index (the column index is calculated from it)

k : split position in the string

// Initialize the entire table.

1. initialize all $X_{i,j}$ to \emptyset

// Initialize the main diagonal from the rules that derive the terminals of the string.

2. **for** $i = 1$ to n

for each variable A

if there is a rule $A \rightarrow x_{i,i}$ **then**

$X_{i,i} := X_{i,i} \cup \{A\}$

// Do for each “diagonal.”

3. **for** $step = 2$ to n

// The cells start from $i, i + step - 1$.

3.1 **for** $i = 1$ to $n - step + 1$

 // Do for each split position.

3.1.1 **for** $k = i$ to $i + step - 2$

if there are variables $B \in X_{i,k}, C \in X_{k+1, i+step-1}$, and a rule $A \rightarrow BC$ **then**

$X_{i, i+step-1} = X_{i, i+step-1} \cup \{A\}$

4. **if** $S \in X_{1,n}$ **then**

return TRUE

else

return FALSE